

Numerically Efficient Fatigue Life Prediction of Rocket Combustion Chambers using Artificial Neural Networks

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Abstract

Fatigue life prediction is an essential part of multidisciplinary design studies and optimization loops, but state of the art finite element based methods are numerically inefficient. We overcome this challenge by training an artificial neural network to predict the number of cycles to failure, based on combustion chamber geometry and operational point. To accomplish this, a 2-d finite element analysis generates 250 000 training data samples. The trained network then predicts previously unseen data with a mean absolute percentage error of 6.8 % in less than 0.1 ms per sample compared to up to 5 min with finite element based methods. To the best of our knowledge, this publication is the first to successfully apply machine learning to fatigue life prediction.

1. Introduction

Future launch systems will most likely be reusable, thus saving costs and conserving resources by not building new flight hardware for every launch. Reusing the first stage engine is particularly effective as it is responsible for a large fraction of total launch costs.¹¹ However, reusability poses new challenges and requirements to the engine: it has to withstand a large number of start-ups (up to 100), resist additional forces during re-entry, and be constructed from light-weight structures.^{7,9} For liquid rocket engines, the main combustion chamber and the turbopumps are the most critical subsystems of the engine limiting its operational time.²⁰

During cyclic operation, extreme thermal and mechanical loads stress the inner wall of a regeneratively cooled combustion chamber. This common cooling technique induces large temperature gradients across the chamber wall, yielding thermal stresses that are usually beyond the elastic limit of the copper alloy used for the inner wall. Additionally, the pressure difference between combustion chamber and cooling channel induces further mechanical loads. These immense thermal and mechanical loads cause inelastic strain, accumulating with each operational cycle until failure of the combustion chamber. As a result, fatigue life estimations are a primary concern for reusable engines. Thus, a considerable amount of literature has focused on a precise understanding of the failure mechanisms and the development of methods estimating the number of cycles until failure.^{13,17,19,21,23}

Precise state of the art fatigue life methods, however, require a numerically expensive finite element analysis of all cycles until failure. Especially for reusable engines with high fatigue life, this leads to prohibitively large computational time requirements, which prevent more sophisticated, multidisciplinary design studies. One step to reduce this effort is to calculate only the very first loading cycle and estimate the fatigue life in a post processing step.¹⁹ This approach can be utilized to study implications of engine cycle variants, propellant combinations, and operating regimes on fatigue life expectancies,²⁵ or to optimize an initial engine design.¹² However, these finite element based methods still require too much numerical effort to be integrated in a system analysis tool, e.g. EcosimPro/ESPSS or to perform multidisciplinary design studies.

Modern machine learning methods, e.g. artificial neural networks, offer a potent possibility to further reduce the numerical effort. These methods, which can be interpreted as statistical analyses, learn fundamental relationships and patterns from data. By constructing surrogate models using samples of the computationally expensive calculation, it is possible to achieve high precision and a computationally cheap prediction. However, it is crucial that the surrogate model imitates the behavior of the simulation model as closely as possible and generalizes well to previously unseen

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data. Neural networks are known to be effective function approximators and have been successfully applied as surrogate models even for high dimensional problems.^{4,14,24} Besides their computational benefits, the process of data fusion and transfer learning additionally allows to integrate multiple data sources, e.g. simulation and experimental data, into the training process in a systematic way. Finally, an optimization loop or a system analysis tool, can utilize such machine learning methods for multidisciplinary design studies.

In this paper, we train a neural network to tackle the challenge of numerically efficient fatigue life prediction. The network is trained with data generated by a finite element method for the first loading cycle followed by a fatigue life estimation during post processing that includes Coffin-Manson theory and ductile failure. The paper discusses the feasibility of this approach, describes the applied model architecture and training process, and compares the performance with the Coffin-Manson/ductile failure method. Our methodology of applying modern data-based machine learning algorithms for numerically efficient fatigue life analysis is the main focus of this work.

Methodology

The following part describes the necessary steps for a successful application of a neural network for fatigue life predictions of liquid rocket engine combustion chambers. First, we have to choose the right set of input parameters for the network. These inputs must contain all necessary information that are relevant for the underlying physical problem. Second, we select the number of cycles to failure as the output to be predicted by the model. Third and potentially most important is to generate a sufficient large and unbiased training data set. Hence, we rigorously analyze the generated fatigue life data. The number of cycles to failure should predominately be in the range that is most relevant for real applications. Furthermore, input variables should cover the entire domain of interest, as neural networks have best performance with their training data range. Finally, the model's performance is rigorously evaluated and compared with the finite element based method. By splitting the data into a training and validation set, we ensure that the NN has generalized to previously unseen data and thus learned the fundamental physical relations of combustion chamber fatigue. Different regularization techniques and network architectures are tested to counter overfitting, which often is a challenging problem in machine learning tasks.

2. Fatigue Life Analysis

As pointed out in the introduction, just the very first loading cycle of the engine is modeled with a finite element analysis and the fatigue life is calculated in a post processing step. This section shortly describes the characteristics of one such engine loading cycle, which consists of four different phases:

- During pre-chilling, the combustion chamber material contracts while it is cooled. The contraction of the inner liner is constraint by the still warmer outer shell, due to different coefficients of thermal expansion of the inner copper alloy and the nickel material of the outer shell. This constraint contraction imposes tensile stresses in the inner liner.
- During the second phase, the hot-run phase, the reverse takes place. The hot inner wall tries to expand but is constrained by the cooler nickel shell, which imposes its contraction to the inner copper liner as it is thicker and has a higher yield strength compared with the copper alloy. As a result, large compressive strains are induced in the inner wall causing the material to plastically deform.
- In the third and fourth phases, i.e. the post cooling and rest phase, tensile stresses reappear in the inner wall.

As soon as one loading cycle is calculated, the maximum strain difference and the remaining plastic straining of this cycle are used to calculate the fatigue life in a post processing step (see section 2.2).

2.1 Thermal and Structural Analysis with ANSYS

This section shortly describes the 2-dimensional finite element analysis with ANSYS Mechanical 18.2 and the applied boundary conditions. The fatigue life is calculated for a single chamber wall section: this section might be the nozzle throat, but the simulation is not limited to this specific section. It can be used for the entire combustion chamber length. Due to symmetry, it is sufficient to model only one half of the channel in the simulation, which lowers the computational effort. Based on the conventional manufacturing process of combustion chambers, cooling channels are machined into the inner liner. Then, the channels are galvanically closed out with a copper layer and an additional stiffer nickel jacket, which contains the pressure and transmits thrust loads.

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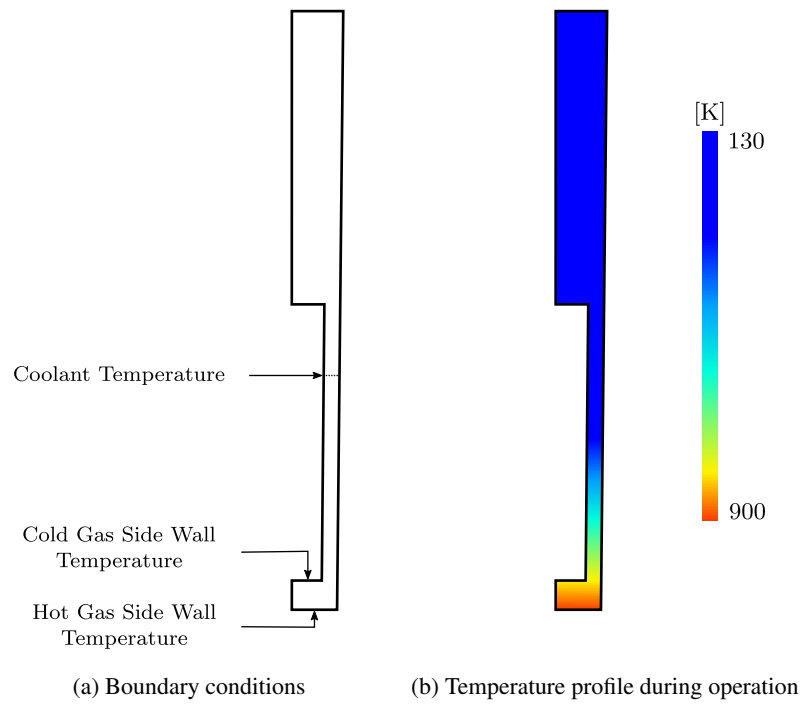


Figure 1: Boundary conditions and results of the thermal analysis

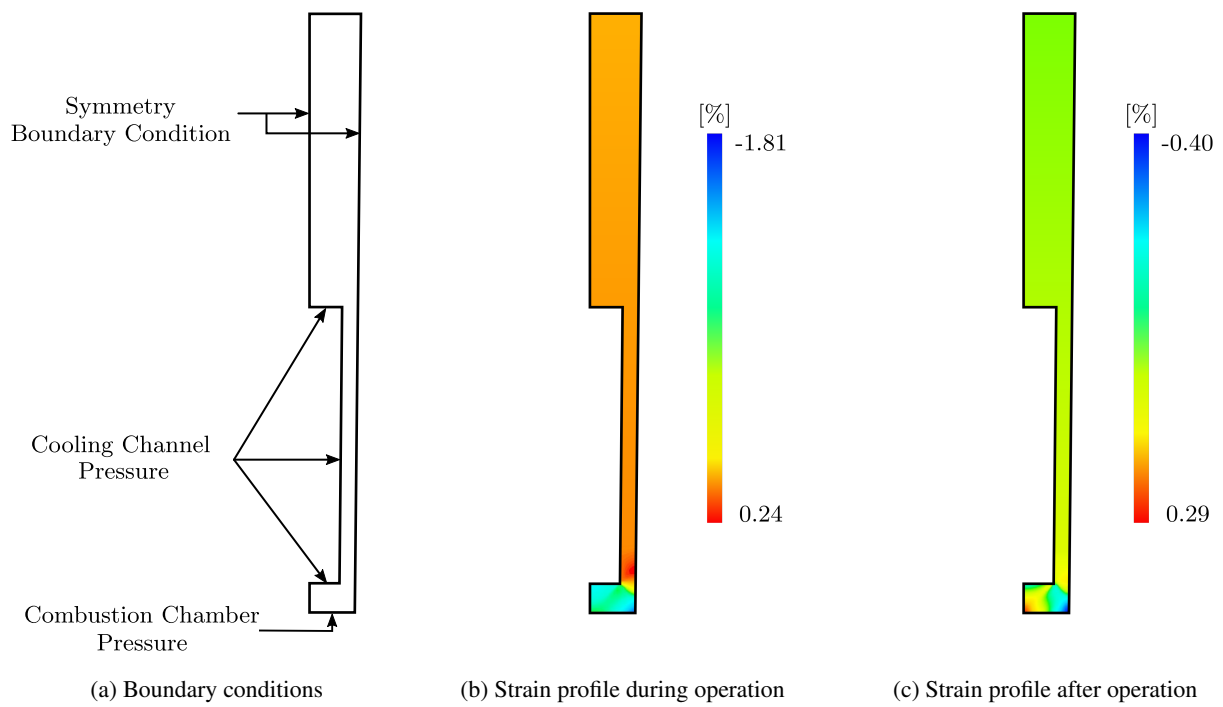


Figure 2: Boundary conditions and results of the structural analysis

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For thermal analysis, the outer shell temperature and the hot-gas- and cold-gas-side wall temperatures are used to determine the temperature distribution during each of the four different engine operation phases (see figure 1b). For simplicity, a linear temperature decrease from the hot-gas side wall to the outer shell is assumed. Figure 1a shows the temperature boundary conditions used for thermal analysis.

For structural analysis, the wall temperature distribution in each loading phase is applied as boundary condition. Further boundaries are given by the pressure difference between combustion chamber and cooling channel. The material parameters for the inner wall, which is made from a high strength copper alloy, were obtained from low-cycle fatigue experiments with a strain amplitude of 2 %.^{3,19} The elasto-plasticity of the wall material is modeled according to the rate independent version of the Chaboche model with kinematic hardening and isotropic softening for $T = 900$ K and additional isotropic hardening for $T = 300$ K, $T = 500$ K and $T = 700$ K. Figure 2 provides an overview of the structural analysis. As the strain profile after operation (figure 2c) shows, plastic straining remains in the wall material after one loading cycle. In summary, the 2-d structural finite element analysis calculates the maximum strain difference and the remaining plastic straining in the inner liner, which is then used in the post processing step.

2.2 Fatigue Life Prediction

The fatigue life estimation in this paper is based on the temperature depended Coffin-Manson law for low cycle fatigue with ductile failure. The 2-d structural finite element analysis provides the minimum strain ϵ_{\min} , the maximum strain ϵ_{\max} , and the remaining strain at the end of the first cycle ϵ_{end} . Based on these strains, the temperature dependent number of cycles to failure $N_{\text{LCF, CoffMans}}(\Delta\epsilon, T)$ is determined with the Coffin-Manson law. The fatigue usage factor $u = 1/N$ represents the maximum fatigue life of the material and must not exceed 1. The temperature dependent ratcheting usage factor $u_{\text{ratch}}(\epsilon_{\text{end}}, \epsilon_{\text{ult}}(T))$ caused by ductile failure is defined by

$$u_{\text{ratch}}(\epsilon_{\text{end}}, \epsilon_{\text{ult}}(T)) = \frac{\max(0, \epsilon_{\text{end}})}{\epsilon_{\text{ult}}(T)}, \quad (1)$$

with the temperature dependent ultimate strain of the chamber wall material $\epsilon_{\text{ult}}(T)$. In order to determine the cumulative usage factor $u_{\text{total}}(T)$, both partial usage factors are summed up:

$$u_{\text{total}}(T) = \frac{1}{N_{\text{LCF, CoffMans}}(\Delta\epsilon, T)} + \frac{\max(0, \epsilon_{\text{end}})}{\epsilon_{\text{ult}}(T)}. \quad (2)$$

u_{ratch} considers the accumulation of tensile plastic strains during cycling loading. Finally, the total number of cycles to failure is defined by:

$$N_{\text{LCF, total}}(T) = \frac{1}{u_{\text{total}}(T)}. \quad (3)$$

By including ratcheting effects, the combustion chamber failure occurs at the symmetry line of the cooling channel. This failure mode, the so-called doghouse effect, is common in regeneratively cooled combustion chambers and has been observed experimentally.¹⁸ In this phenomenon, the inner hot-gas side wall becomes thinner and finally fails by bulging out towards the interior of the combustion chamber.

3. Artificial Neural Networks

In recent years, a considerable amount of literature has been published on neural networks. The well known publication by Goodfellow et al.⁶ provides an in-depth analysis of machine learning, covering both theory and practical application. It serves as basis for this chapter and is recommended for deeper insights into machine learning. This section gives a short introduction, summarizes the theory and explains the application of neural networks to fatigue life prediction.

In general, machine learning is the capability of a system to acquire its own knowledge by extracting information and patterns from raw data. Providing the right data to a machine learning algorithm can enable it to solve various problems such as image recognition or predictive analytics. Because the algorithm extracts its knowledge from the given data, it improves with more data and experience. Deep learning is a special approach to machine learning that tries to learn complicated relationships by building them out of simpler, less complex pieces of information. A nested hierarchy of this concept breaks down complicated problems in different simpler, more abstract representations of the original problem. Because this concept usually results in many sequential computational layers, it is called deep learning.

3.1 Theory of Artificial Neural Networks

Inspired by the biological brain, deep learning methods are often referred to as artificial neural networks because of a similar information processing.⁶ In general, such network consists of an input layer, multiple hidden layers and an output layer, which are all built out of simple elements called neurons. Each neuron receives inputs from the previous layer, calculates the weighted sum of these inputs according to some model parameters, and applies a nonlinear transformation to this sum to generate its output. Connections between two layers transfer the output of previous neurons to the input of the next layer. Each connection between two neurons is assigned a weight w . The strategy of deep learning is to learn these weights – the model parameters – so that the network can approximate some function f^* that represents the underlying physical problem. Among other things, neural networks can be used for regression and classification problems.

In classification, a network separates the data into multiple categories k depending on the input vector, which means the algorithm is asked to output a discrete function $f : \mathbb{R}^n \rightarrow \{1, \dots, k\}$. Well-known examples of classification are object recognition in images, speech recognition, or data clustering. In regression problems, the network estimates a numerical value for a given input vector with dimension n as output of the function $f : \mathbb{R}^n \rightarrow \mathbb{R}$. Regression algorithms owe their name due to their continuous output space.

3.1.1 Neuron Operation

As explained above, neural networks are made of many elementary units called neurons. In general, every neuron computes the weighted average of its input, passes this sum through a nonlinear activation function and sends the output to the following layer. Mathematically speaking, every neuron in a hidden layer has an input vector $\vec{a}^{(0)} = (a_1, a_2, \dots, a_n)$ and a weight vector $\vec{w} = (w_1, w_2, \dots, w_n)$, where n is the number of inputs to the neuron. The activation function ϕ describes a nonlinear transformation on the weighted sum so that the model can capture nonlinear features of the data. The output $a^{(1)}$ of a single neuron can then be written as

$$a^{(1)} = \phi \left(\sum_{i=1}^n w_i a_i^{(0)} + b \right). \quad (4)$$

In recent years, many different activation functions have been used for deep learning. A common example of a nonlinear activation function is the logistic sigmoid function or the rectified linear unit (ReLU) activation function. Using vector notation, the output of each hidden layer can be written as

$$\vec{a}^{(1)} = \phi \left(\vec{w} \vec{a}^{(0)} + \vec{b} \right), \quad (5)$$

where \vec{w} and \vec{b} represents adjustable parameters of all neurons in this layer, while $\vec{a}^{(0)}$ is the output vector of the previous layer. In summary, a neural network can be seen as a function $y = f(x, \theta)$ with parameters θ . The strategy of deep learning is to adjust these parameters so that the network can approximate the fundamental relationships of the given task. Gradient descent is by far the most common learning strategy.

3.1.2 Gradient Descent

During training or learning, the model requires a measure for the quality of its prediction to adjust its parameters. In regression problems, one of the simplest and most effective measure is the quadratic cost function. It returns the sum of squared errors between predicted value and ground truth:

$$J(\theta) = \frac{1}{2m} \sum_{i=1}^m (y_i - f(x_i, \theta))^2. \quad (6)$$

Here, x_i and y_i are input and ground truth of a data point, m is the total number of data points and $f(x_i, \theta)$ denotes the predicted output from the network according to its parameters θ . In fact, training can now be seen as finding optimal parameters θ such that the loss function J is minimal, which is a classical optimization approach.

Gradient descent is by far the most popular optimization strategy in deep learning to find the minimum of the cost function. It can be summarized by computing the slope or gradient vector of the cost function and then taking a step proportional to the negative gradient towards the local minimum. In other words, the learning algorithm will shift the

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trainable parameter of the network by a small fraction (the learning rate ϵ) of the computed gradient, according to the gradient vector. Mathematically speaking, gradient descent calculates a new parameter vector

$$\vec{\theta}' = \vec{\theta} - \epsilon \nabla_{\theta} J(\vec{\theta}), \quad (7)$$

where $\nabla_{\theta} J(\vec{\theta})$ is the gradient of the cost function with respect to model parameters θ . However, the gradient calculation can become computational expensive for larger data sets and a substantial network size. Thus, the gradient vector is calculated in a more efficient way called mini-batch gradient descent. It is an variation of the classical gradient descent algorithm that estimates the gradient on a small batch of a few hundred randomly chosen data points. This process is repeated until the entire data have been used, which is called one epoch. Further information on gradient descent and advanced enhancements are given in the literature.⁶

3.2 Generalization and Overfitting

For a sufficient large number of parameters and a well defined problem, the network will almost always be able to fit the data used for training since it has adjusted its weights accordingly. However, the network must also perform well on new, previously unseen data. The capability to perform well on new data is called *generalization*. Generally, two central challenges can occur while training a network. First, *underfitting* (figure 3a) indicates that the model capacity is too small because the network is not able to adjust its parameters for a sufficient small error on the training data (another reason could be too much regularization). Second, in case of *overfitting* (figure 3c), the network has just memorized the training data, but has not learned the fundamental relationships of the problem, thereby it has no general applicability. For an appropriate model capacity (figure 3b), the network has learned the mapping between input and output.

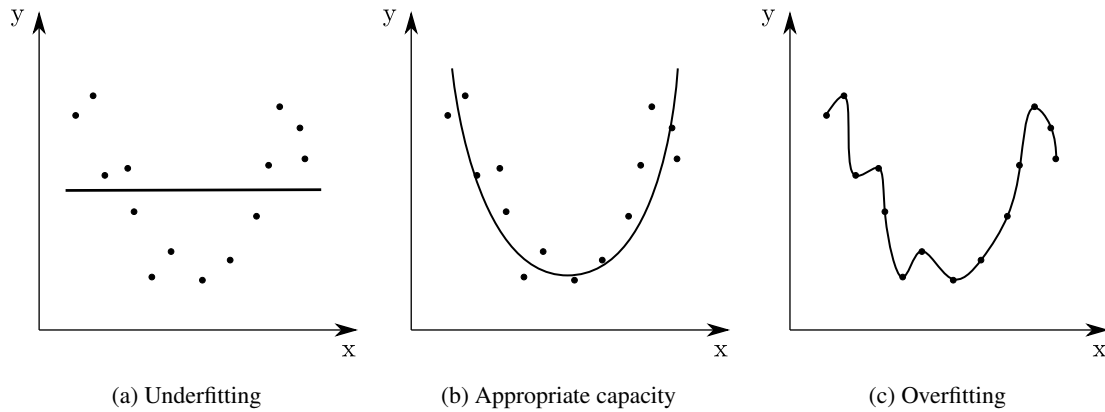


Figure 3: Capacity, underfitting and overfitting of a neural network⁶

For complex problems it is impossible to guess the right model architecture, e.g. number of layers or neurons, before actual training. Furthermore, it is clear that an overfitting model is worthless for future use because it cannot predict new data. Therefore, careful evaluation of the trained network is necessary. For this reason, the data set is commonly split into three different subsets.⁶ The training set is used to adapt and modify the network's weights and biases during training. The second data set – the validation or development set – exists to perform hyperparameter tuning, to select the best network architecture, to achieve a good balance between network's performance and to avoid overfitting. However, the error rate of the final model on validation data will be biased since this data was used to tune and select the final model. Thus, a third data set, the test set, reveals the performance of the final model, but is not used to change the model.

In case of overfitting, the network's performance differs significantly between training and validation data. Regularization techniques try to reduce this gap, but may increase the train error. A common approach of regularization is to add an extra term to the cost function (equation 8), which penalizes larger network parameters. The most common way of parameter norm penalty is called *L2 regularization* or *weight decay*. The regularized cost function becomes

$$J^*(\theta) = \frac{1}{2m} \sum_{i=1}^m (y_i - f(x_i, \theta))^2 + \lambda \sum_{j=1}^n \theta_j^2, \quad (8)$$

where λ is an additional hyperparameter that controls the amount of regularization and n gives the total number of network parameters. When talking about neural networks as an optimization problem, the model now tries to minimize both its parameters and the training error. In general, smaller model parameters prevent overfitting, thus improving generalization. Additional regularization techniques, such as dropout,^{1,22} early stopping¹⁶ or adding noise to models²⁶ can further increase the generalization ability. Only weight decay was used for the network presented in this publication, but other techniques can be interesting for deeper networks or cases with less data.

4. Neural Network for Fatigue Life Prediction

This section presents the neural network for fatigue life prediction, describes how to find the optimal network architecture, discusses the training process, and analyzes the data used for training.

4.1 Data Generation

In general, a balanced and evenly distributed data set boosts the chance of successfully applying neural networks to complex problems. Therefore, we carefully create and analyze two separate data sets for methane and liquid hydrogen. We focus on methane, because it is the promising propellant in terms of fatigue life expectancy. Nevertheless, we similarly train and evaluate a second neural network for liquid hydrogen.

4.1.1 Methane Data Set

The methane data set consists of 130 000 fatigue life samples. Table 1 gives an overview of the inputs for thermal and structural analysis, and shows the minimum, maximum and mean value of each variable in the generated data set. These lower and upper limits cover the geometrical dimensions and operation conditions of both first and upper stage liquid rocket engines and are representative for the entire combustion chamber length including the nozzle throat, which experiences the highest thermal stresses. During data generation, parameter combinations are randomly sampled within the given limits.

Table 1: Parameter distribution of the methane data set

| Parameter | Min | Max | Mean |
|---|-----|------|------|
| Chamber Pressure [bar] | 25 | 300 | 129 |
| Pressure Loss [%] | 10 | 120 | 55 |
| Heat Flux Density [MW m ⁻²] | 5 | 125 | 64 |
| Chamber Radius [mm] | 20 | 300 | 97 |
| Outer Shell Thickness [mm] | 7 | 25 | 13 |
| Outer Shell Temperature [K] | 110 | 600 | 286 |
| Hot-Gas Wall Temperature [K] | 600 | 1100 | 900 |
| Channel Area [mm ²] | 1 | 20 | 9 |
| Channel Aspect Ratio [-] | 0.3 | 15 | 6.2 |
| Wall Thickness [mm] | 0.4 | 1.6 | 1.0 |
| Fin Thickness [mm] | 0.5 | 8.0 | 2.3 |

Note that further variables can be easily derived. For example, heat flux density and hot-gas wall temperature determine the cooling channel wall temperature when assuming linear one-dimensional heat conductivity in the wall material. Coolant pressure in the channel cross section is given by the combustion chamber pressure and the pressure loss: $p_{\text{cooling channel}} = (1 + \text{pressure loss}) \cdot p_{\text{combustion chamber}}$. The fin thickness is determined by the number of cooling channels for a given chamber radius and channel width. The outer shell is at coolant bulk temperature, which is suitable for most realistic operation conditions.

4.1.2 Hydrogen Data Set

The hydrogen data set is comparable in size and variable distribution to the methane set. It consist of approximately 120 000 data points, sampled from the distribution in table 2. Using liquid hydrogen at lower temperatures than methane, the minimal outer shell temperature is consequently lower. The resulting mean number of cycles to failure is 131, while the first and third quartile are at 46 and 191, respectively. Note that the resulting fatigue life for liquid

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hydrogen is slightly lower compared with methane. This can be explained due to the lower outer shell temperature resulting in higher temperature gradient within the copper liner and thus larger thermal loads on the liner material.

Table 2: Parameter distribution of the liquid hydrogen data set

| Parameter | Min | Max | Mean |
|--|-----|------|------|
| Chamber Pressure [bar] | 25 | 300 | 134 |
| Pressure Loss [%] | 15 | 120 | 64 |
| Heat Flux Density [MW m^{-2}] | 5 | 130 | 68 |
| Chamber Radius [mm] | 20 | 250 | 109 |
| Outer Shell Thickness [mm] | 7 | 25 | 13 |
| Outer Shell Temperature [K] | 30 | 600 | 230 |
| Hot-Gas Wall Temperature [K] | 550 | 1100 | 892 |
| Channel Area [mm^2] | 1 | 20 | 9 |
| Channel Aspect Ratio [–] | 0.5 | 15 | 7.3 |
| Wall Thickness [mm] | 0.4 | 1.6 | 1.0 |
| Fin Thickness [mm] | 0.5 | 8.0 | 2.6 |

4.2 Data Analysis

With regard to data analysis, a histogram and box-and-whisker plot without outliers give a brief summary of the resulting fatigue life data distribution (figure 4). For methane and the chosen boundary conditions, the mean number of cycles to failure is 145, while the first and third quartile are at 57 and 203, respectively. Over the entire data set, number of cycles to failure range from 1 to 500. We excluded samples with higher fatigue life, since the focus is to predict the fatigue life of the most critical sections of a liquid rocket engine. In summary, both boundary conditions and number of cycles to failure cover a reasonable range of realistic liquid engine operation conditions.

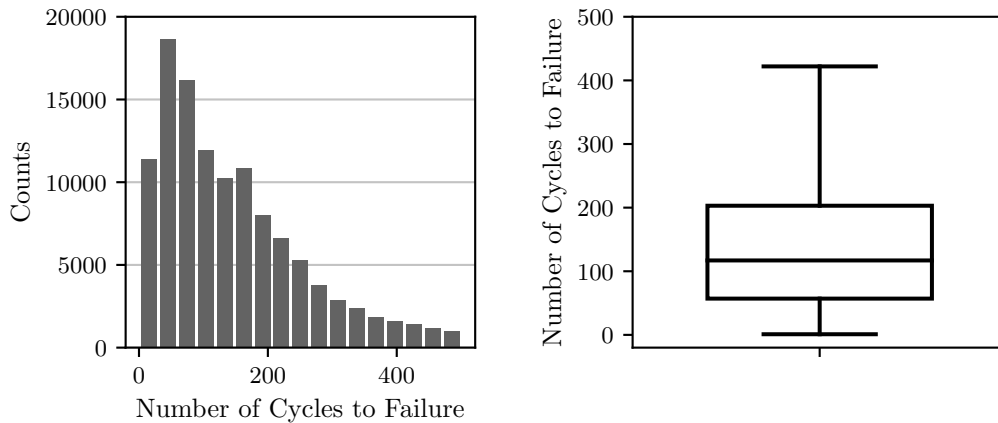


Figure 4: Data distribution of the methane data set

4.3 Network Architecture and Training

We propose a fully-connected, feed-forward network for fatigue life prediction. Figure 5 shows an exemplary model with two hidden layers, four neurons per layer and all input parameters. Although there are only very few hidden neurons in this example, the network already has 64 trainable weights. Obviously, the number of parameters considerably increases with more layers and neurons.

During training, the weight update is calculated with the *Adam*¹⁰ optimizer, which extends the classic stochastic gradient descent algorithm. Overfitting is prevented using L2-regularization. For faster and more robust learning, all inputs are automatically scaled and standardized with the *StandardScaler* from *SCIKIT-LEARN*.¹⁵ The model is programmed with the widely known *KERAS*⁵ deep learning library written in *PYTHON*. *KERAS* is a high-level neural network framework that uses *TENSORFLOW* as its backend.

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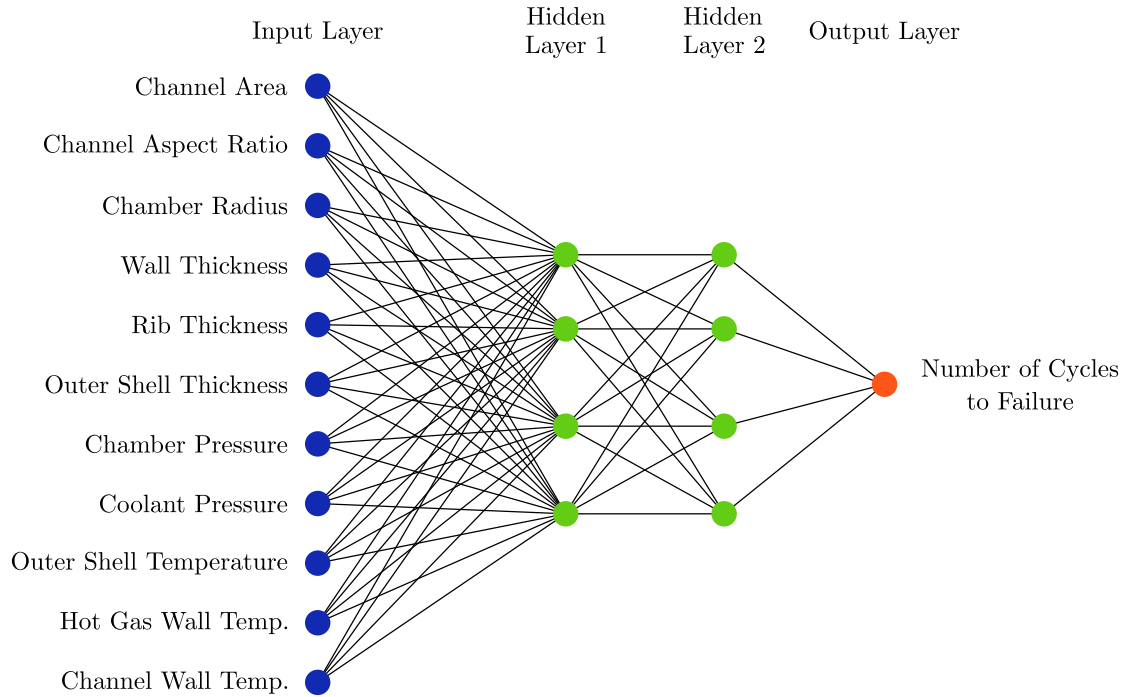


Figure 5: Exemplary network architecture with 2 fully connected hidden layers

As discussed, there is no general strategy to determine the network's architecture in advance. Thus, we use random search to find the best network architecture and training parameters. Bergstra and Bengio² showed that a random search algorithm performs as well as classical grid search but with less computational effort. To compare different hyperparameter combinations, we use k-fold cross validation to assess the network's performance during random search. Cross validation is a re-sampling procedure that split the entire data set into k separate groups. Then, the network is trained on k-1 subsets, while the performance is evaluated on the remaining subset. This procedure is repeated k times, such that each subset is used for evaluation once. Finally, the algorithm averages the performance across all subsets. For this paper, we use 5-fold cross validation for in total 500 different hyperparameter combinations and network architectures.

Summarizing the hyperparameter optimization, a network with 3 hidden layers, 250 neurons per layer and a weight decay rate of 0.06 achieves the overall best performance on both training and validation data. Each layer uses a Leaky ReLU nonlinear activation function and ADAM updates the weights with a learning rate of 0.01. Training for 750 epochs with a batch size of 4096 takes about 5 minutes on a NVIDIA QUADRO P4000 GPU.

5. Results and Discussion

Having discussed the theory of neural networks and how to apply them to fatigue life prediction, this final section of the paper evaluates the network's performance and visualize the training results. Since we must ensure general applicability of the network, validation and test sets with 15 000 samples each were set aside and not used to adjust any weights during training. For further validation and understanding, heat maps visualize the network output.

5.1 Training and Validation

Figure 6 compares predicted and target number of cycles to failure for all three different data sets. Points situated on the angle bisector are predicted perfectly. It can be seen that the proposed network achieves high precision in fatigue life prediction. Overall, the model estimates the number of cycles to failure with a mean squared error (MSE) of 233 on previously unseen data (equal to a mean percentage error of 6.8 %). Since the network has optimized its weights according to the training data, its performance is thereby slightly better on those data samples (MSE of 80). By increasing the amount of regularization, it is possible to decrease the difference between train and test error. However, this would also decrease the overall performance of the network. Hence, we choose this model architecture with the best performance on the validation data and further evaluate its generalization capabilities.

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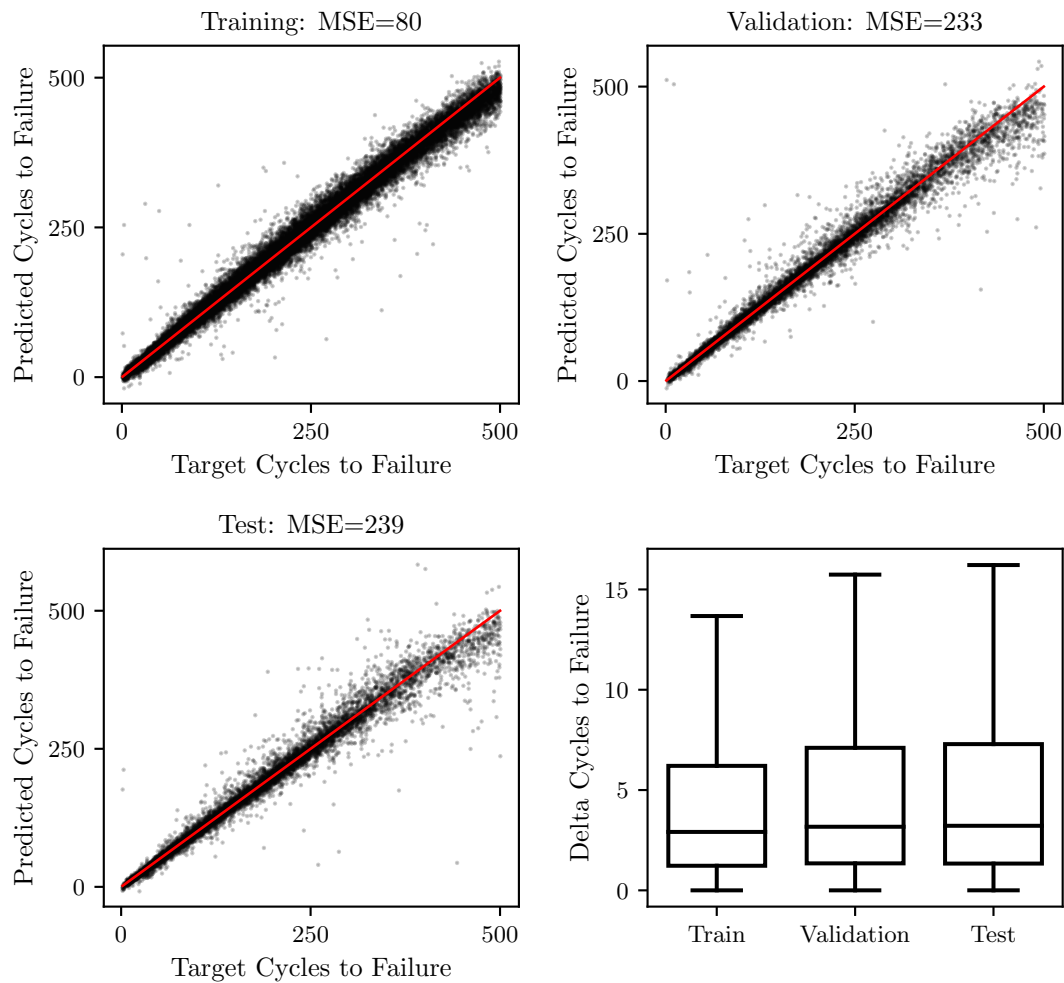


Figure 6: Training and validation results for the proposed model

The error distribution for test and validation data suggests that the network is slightly more precise for data samples with lower rather than higher fatigue life. A possible explanation for this might be that the post processing method used for data generation only considers the very first loading cycles and estimates the fatigue life with the resulting plastic straining. Consequently, the post processing method should be more accurate for low fatigue life and thus generate better data with lower variance in this region. Therefore, after learning the fundamental physical relationships, the network is more accurate for lower fatigue life. Since we want to predict the fatigue life of the most critical sections of a liquid rocket engine, it is desirable to have the best performing network for low fatigue life.

As Figure 6 shows, there are few data points with a significant difference between target and predicted fatigue life. Since there are only very few outliers compared to the overall data set size – and neural networks are in general quite robust to few outliers⁸ – these points will not deteriorate the performance of the network.

5.2 Response Visualization

Finally, it is often useful to visualize the model in action instead of just looking only at the performance measurements such as validation loss (mean-squared-error). Directly observing the outputs helps to decide whether a model has learned the fundamental physical relationships of the given task or if it merely memorizes the training data. Additionally, it is important to visualize how the model performs in between of given input data. That said, we need to evaluate the model for various different input parameters.

Heat Map

A heat map is a visualization technique that shows the model's answer to given inputs. In other words, it can be described as a parametric study in which two inputs change while all other parameters are kept the same. The output, i.e. the number of cycles to failure, is then plotted in a two-dimensional scatter plot, where both free inputs are used as x- and y-axis. The analysis of this heat map can identify possible problems in terms of overfitting. For example, further investigations would be necessary for regions with strong discontinuities or peaks in fatigue life where we do not expect such peaks from our physical understanding.

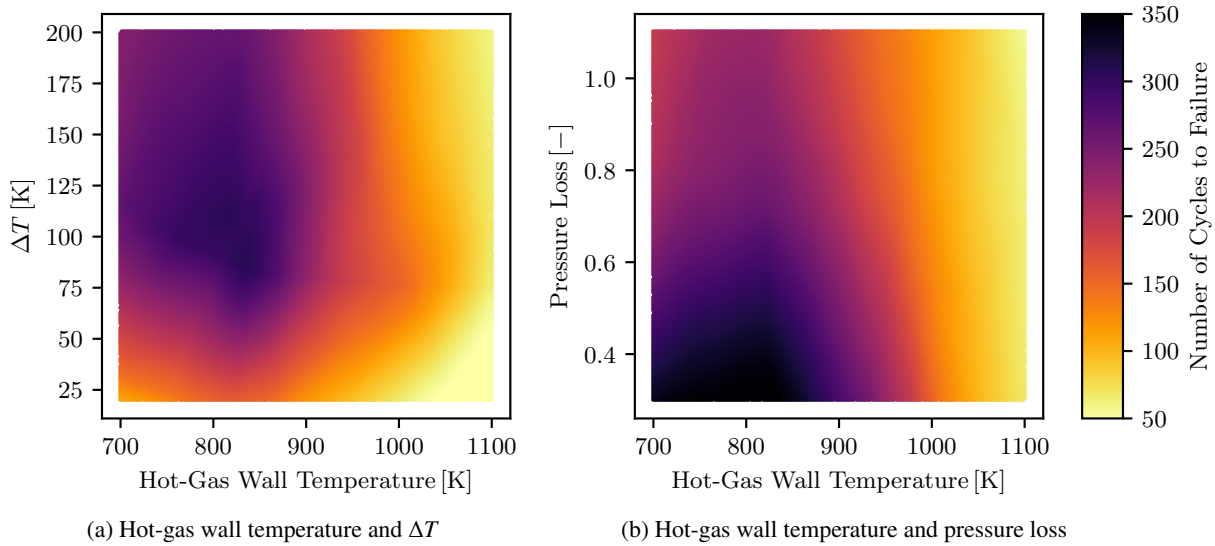


Figure 7: Heat map of the trained network. If not varied on either axis, the following boundary conditions were used: chamber pressure 120 bar, chamber radius 50 mm, channel area 5 mm², channel aspect ratio 5, outer shell thickness 10 mm, rib thickness 1 mm, hot-gas wall thickness 1 mm, outer shell temperature 150 K, ΔT 200 K, pressure loss 0.6.

Figure 7 illustrates the response for two generic test cases. ΔT denotes the temperature difference between hot-gas side wall and cooling channel wall and pressure loss represents the percentage difference between cooling channel and combustion chamber pressure: $p_{\text{cooling channel}} = (1 + \text{pressure loss}) \cdot p_{\text{combustion chamber}}$. In terms of physical understanding, the network's response seems reasonable as there are no sharp gradients or discontinuities in the predicted fatigue life. Furthermore, the network calculates a low number of cycles to failure for high hot-gas wall temperatures in combination with a low temperature difference (see figure 7a). In this region, the entire inner wall structure is at high temperatures, yielding poor mechanical properties of the wall material. Likewise, fatigue life increases with lower structural temperature.

As pointed out in section 1, the mechanical loads due to pressure differences are usually secondary. The primary influence on the fatigue life is given by the thermal loads. Hence, only for lower thermal loads (i.e. lower hot-gas wall temperatures) mechanical loads become more dominant. This behavior is comparable to the predicted fatigue life in figure 7b. For higher wall temperatures, the predicted number of cycles to failure predominantly change with wall temperature, whereas the pressure loss is important for lower wall temperatures.

Comparison with the Finite Element Method

In this section, the hot-gas side wall temperature and the outer shell temperature is separately varied to see how they affect fatigue life. Figure 8 compares the results of the neural network with the finite element method. It can be seen that the proposed network achieves high precision in fatigue life prediction. It has modeled the fundamental physical mapping from input to output. Whereas the predictive error is minor for higher hot-gas wall temperatures, it increases for values smaller than 750 K. However, our choice of training data explains this deviations. Since we exclusively trained the model on samples with less than 500 cycles to failure, it has to extrapolate for very low wall temperatures. Because neural networks are generally unable to extrapolate properly, the error increases.

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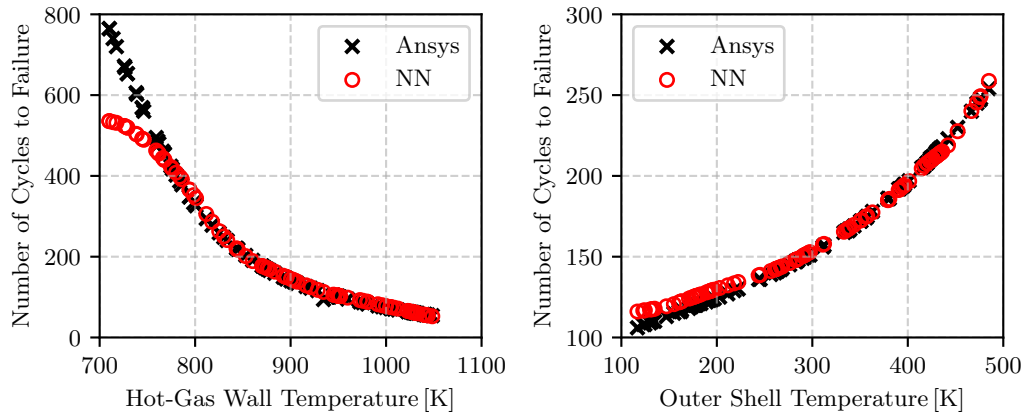


Figure 8: Predictive performance of the network. If not varied, the following boundary conditions were used: chamber pressure 80 bar, chamber radius 26 mm, channel area 5 mm², channel aspect ratio 5, outer shell thickness 10 mm, rib thickness 1 mm, outer shell temperature 220 K, hot-gas wall temperature 900 K, ΔT 150 K, pressure loss 0.25. Scales of subfigures differs.

Summarizing the training results, the heat maps and the parametric study, the proposed model has modeled the fundamental relations of fatigue life prediction and generalizes well to previously unseen data. For a reliable prediction, we only have to ensure that the data sample we want to predict is from the same distribution as the training data.

5.3 Influence of Data Set Size

In machine learning, the amount of available data often determines the performance of the algorithm. However, it is hard to estimate how much data is necessary to approximate the unknown underlying function from inputs to outputs. The required amount of data depends on many factors, such as the complexity of the problem or the actual machine learning algorithm. In general, too little data will more likely result in poor performance on new, previously unseen data.⁶ A common strategy to determine the amount of data for a specific problem is to evaluate the network's performance on different data set sizes for a fixed network architecture. The resulting curve, often referred to as learning curve, shows the cross-validated training and validation score for different training set sizes.

As the learning curve in figure 9 shows, the model performance on the validation set steadily increases with more training examples and will likely convergences to a plateau at which the model will not benefit from more data. Based on the gradient of the learning curve, we can conclude that the amount of trainings data is sufficient for high precision.

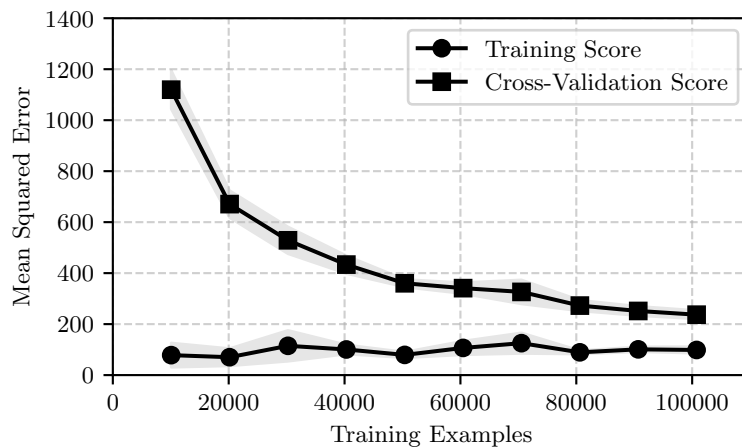


Figure 9: Learning curve of the network and standard deviation for different cross-validation splits (transparent area)

5.4 Hydrogen Data Set

Using the same architecture and validation process (section 2.2 and chapter 5), we trained a second model for liquid hydrogen. The model fits the data with a mean squared error of 93, 264 and 290 on validation, training and test data, respectively. These results correspond to a mean absolute percentage error of 7.2 % on previously unseen data. Summarizing the validation, we can conclude that a neural network performs equally as well for liquid hydrogen as it does for methane.

5.5 Performance measurement

The overall goal of this research was to develop a numerically efficient method for fatigue life prediction of liquid rocket engine combustion chambers. Although neural networks require a time-intensive learning phase and a large amount of training data, their predictive speed is high because the network only has to multiply the input vector with its weight matrices to generate the output. Additionally, the numerical effort does not depend on the actual value of the inputs (e.g. size of the combustion chamber), whereas finite element based methods do need increasingly more time with larger model sizes and thus higher number of mesh elements.

On a computer with an INTEL XEON W-2123 CPU, fatigue life analysis with ANSYS MECHANICAL takes approximately 2 to 5 minutes depending on the model size. In contrast, the neural network computes 1 000 000 data samples in 12 s on the same CPU, which is an average of 12 μ s per calculation. This comparison shows the great potential of such data-driven methods for multidisciplinary design studies or optimization loops.

6. Summary and Outlook

In this paper, an artificial neural network was successfully trained to predict the fatigue life of liquid rocket engine combustion chambers. The network was trained on data generated by a finite element method for the first loading cycles combined with a post processing approach to estimate the number of cycles to failure. This approach combines the Coffin-Manson method for low cycle fatigue with ductile failure caused by ratcheting effects during post processing. After training, the proposed neural network predicts previously unseen data with a mean absolute percentage error of 6.8 % and 7.2 % for methane and liquid hydrogen, respectively. Hence, we can conclude that it has closely modeled the underlying relations of fatigue in rocket engine combustion chambers.

In summary, the results have proven the feasibility of applying modern data-based machine learning algorithms for numerically efficient fatigue life estimation. By splitting the data into different subsets for training, validation and testing, we demonstrated the general applicability of the network. Moreover, the proposed network predicts the number of cycles to failure in under 0.1 ms, which is up to 10^7 times faster than classical finite element based methods. Due to this enormous time benefit, a data-based algorithm is well suited to be embedded in a system analysis tool, e.g. EcosimPro/ESPSS. Thus, this numerically efficient method facilitates more sophisticated, multidisciplinary design studies that could optimize an entire engine cycle for maximum fatigue life. Furthermore, the neural network could be used in the design phase of a new engine to optimize the cooling channel geometry or the operating conditions of the engine.

However, modern data-based algorithms (like neural networks) also have natural drawbacks. Due to the high number of parameters, these algorithms often lack a deeper understanding of the fundamental physics. Furthermore, neural networks cannot extrapolate, but only provide reliable and robust predictions within the training subspace. In summary, domain knowledge and the understanding of physical processes will always be crucially important to evaluate and justify the prediction of data-driven algorithms.

Further research could investigate the process of data fusion and transfer learning that allows to integrate multiple data sources into the training, e.g. experimental data. This approach could further improve the network's performance. Using the proposed network, future investigations can analyze fatigue life expectancies for different propellant combinations, operating conditions, or various combustion chamber geometries in the context of reusability. This work is the first time an artificial neural network was trained for fatigue life predictions (to the best of our knowledge). It will hopefully serve as a base for future studies on optimizing an entire engine design for maximum fatigue life.

7. Acknowledgments

It is a pleasure to thank R. Dos Santos Hahn and C. Schorn for comments that greatly improved this paper.

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